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# 1 项目概况

## 1.1 建筑方案

本项目选自第十届高校木结构设计邀请赛赛题，要求主要使用木材作为结构材料，设计一建筑面积约为1850平方米的展览馆。方案中，建筑场地位于上海市。该建筑为主体三层，建筑总体及周围环境渲染图见图1.1。



图 1.1 建筑总体及周围环境渲染图

## 1.2 技术参数

设计使用年限：50 年；

建筑结构重要性等级：二级；

建筑抗震设防类别：丙类；

结构形式：框架结构；

当地基本风压：0.55 kN/m<sup>2</sup>；

基本雪压：0.20 kN/m<sup>2</sup>；

抗震设防烈度 7 度，设计基本地震加速度值为 0.10g，设计地震分组为第一组。

### 1.3 结构方案

运用软件 RFEM6.1 建立结构模型如下图 1.2 所示。

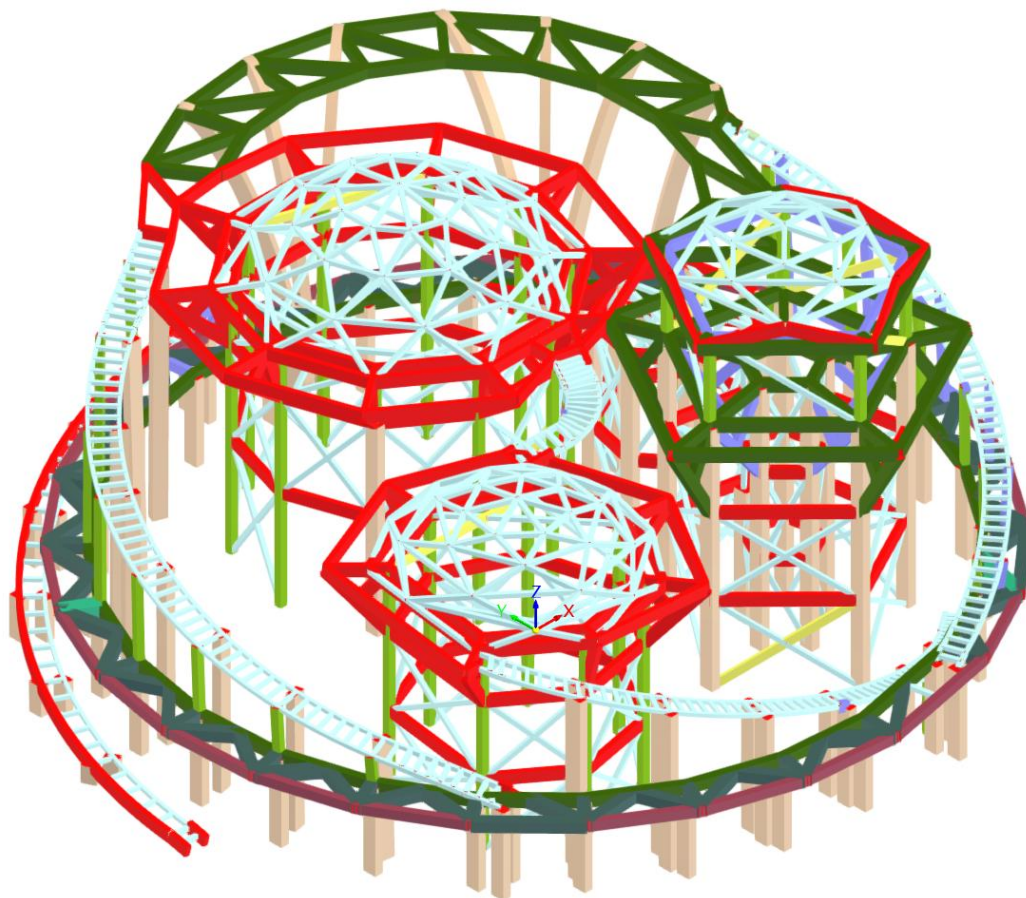


图 1.2 结构模型图

## 2 设计依据

### 1.1 主要设计及施工验收规范及规程

|                     |                     |
|---------------------|---------------------|
| 《建筑结构可靠度设计统一标准》     | (LC1B 50068-2018)   |
| 《工程结构可靠性设计统一标准》     | (LC1B 50153-2008)   |
| 《建筑结构荷载规范》          | (LC1B 50009-2016)   |
| 《工程结构通用规范》          | (LC1B 55001-2021)   |
| 《木结构设计标准》           | (LC1B 50005-2017)   |
| 《木结构通用规范》           | (LC1B 55005-2021)   |
| 《木结构工程施工规范》         | (LC1B/T 50772-2012) |
| 《木结构防火设计标准》         | (T/CECS 1104-2022)  |
| 《建筑抗震设计规范》（2024 年版） | (LC1B 50011-2010)   |
| 《建筑与市政工程抗震通用规范》     | (LC1B 55002-2021)   |
| 《胶合木结构技术规范》         | (LC1B/T 50708-2012) |
| 《钢结构设计规范》           | (LC1B/50017-2017)   |
| 《木结构工程施工质量验收规范》     | (LC1B 50206-2012)   |

国家和上海市的其他相关设计及施工验收规范及规程。

### 2.1 其他文件

竞赛主办方提供的设计用地图片。

3 荷载计算与内力分析

3.1 恒荷载

3.1.1 线荷载

本项目的梁、柱和隅撑所用材料均为同等组合胶合木，根据使用功能不同分别选用不同等级胶合木。所有胶合木自重为  $7\text{kN/m}^3$ ，截面尺寸如表 3.1 所示。使用结构计算软件 RFEM 6.1，计算构件线荷载，再分配到相应的杆件上。

表 3.1 构件截面尺寸

| 构件类型 | 梁       | 柱       | 隅撑      |
|------|---------|---------|---------|
| 截面尺寸 | 300×550 | 200×450 | 400×400 |
|      | 300×650 | 400×500 | 200×200 |
|      | 300×450 |         |         |
|      | 450×600 |         |         |
|      | 200×400 |         |         |
|      | 400×550 |         |         |

3.1.2 面荷载

楼面板为正交胶合木（CLT）板材，厚度为 175mm，胶合木重度为  $7\text{kN/m}^3$ ，面荷载  $LC1_1=7\times0.175=1.225\text{ kN/m}^2$

屋面玻璃部分均采用 12 双层中空玻璃，玻璃重度为  $25.6\text{kN/m}^3$ ，自重面荷载  $LC1_2=25.6\times0.012=0.307\text{ kN/m}^2$ 。

3.2 活荷载

结构中，不上人屋面荷载取  $0.5\text{kN/m}^2$ ，楼面荷载取  $3.0\text{kN/m}^2$ ，走廊、室外露台处活荷载取  $3.5\text{kN/m}^2$ 。

3.3 风荷载

根据《建筑结构荷载规范》LC1B50009-2012，计算结构表面的风压标准值：

$$w_k = \beta_z \times \mu_z \times \mu_s \times w_0$$

式中， $\beta_z$  为风振系数； $\mu_z$  为风压高度变化系数； $\mu_s$  为体型系数； $w_0$  为基本风压。结构所在地基本风压  $w_0=0.55\text{kN/m}^2$ ，场地类型为 B 类，运用 RFEM6.1 荷载向导功能，得到风荷载大小，施加到杆件上。

3.4 雪荷载

根据《建筑结构荷载规范》（LC1B 50009-2016）和《工程结构通用规范》（LC1B

55001-2021)，对于不上人屋面可以单独考虑活荷载或雪荷载，并取两者中最大值进行设计。本项目结构所在地为上海，基本雪压 $S_0=0.20\text{kN/m}^2$ ，小于屋面活荷载，所以结构设计时忽略。

3.5 地震荷载

项目所在地位于上海，根据《建筑抗震设计规范》(2024 年版)(LC1B50011-2010)场地抗震设防烈度为 7 度，地面加速度  $0.10g$ 。将以上系数输入到 RFEM6.1 中，由程序根据振型分解反应谱法进行计算。

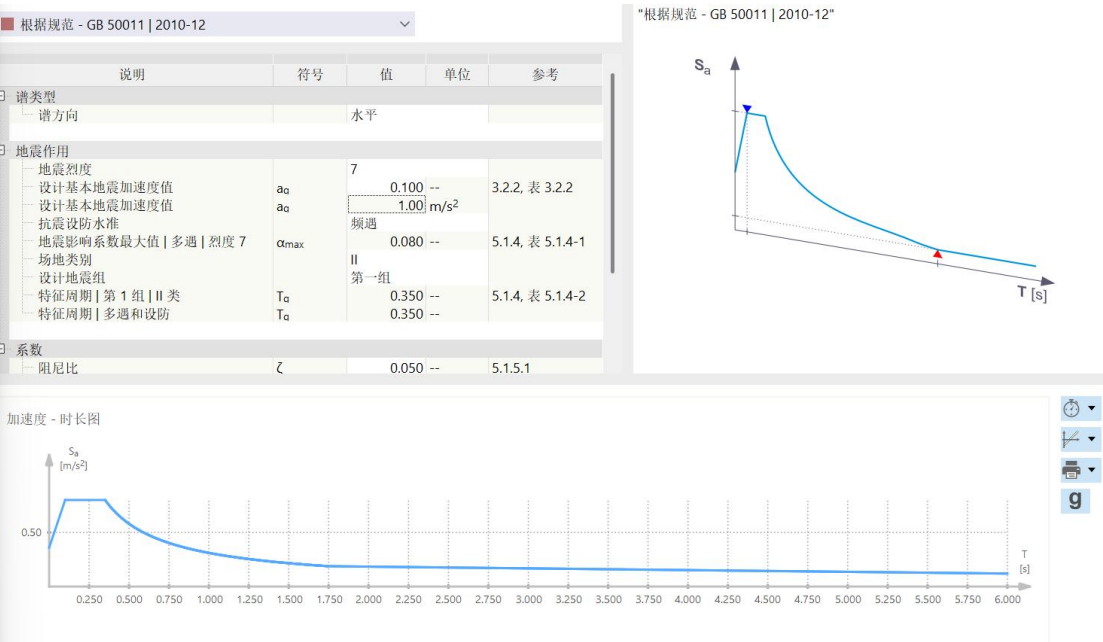


图 3.1 反应谱参数

3.6 荷载组合

3.6.1 基本组合

承载力计算中，选取了以下荷载基本组合进行计算。其中，LC1 为恒荷载；LC2 为活荷载；LC3 为 X 方向风荷载；LC4 为 Y 方向风荷载；

- 1.30LC1
- 1.30LC1+1.50LC2
- 1.30LC1+1.50LC4
- 1.30LC1+1.50LC3+1.05LC2
- 1.30LC1+1.50LC4+1.05LC2
- 1.30LC1+1.50LC3
- 1.30LC1+0.9LC3+1.50LC2
- 1.30LC1+0.9LC4+1.50LC2

### 3.6.2 标准组合

正常使用极限状态下，选取了以下 8 种荷载标准组合进行计算：

LC1

LC1+LC2

LC1+LC3

LC1+LC4+0.70LC2

LC1+LC3+0.70LC2

LC1+LC4

LC1+0.60LC3+LC2

LC1+0.60LC4+LC2

### 3.6.3 偶然组合

对构件进行防火验算时，选取以下 6 种荷载偶然组合进行计算：

1.0LC1

1.0LC1+0.4LC3

1.0LC1+0.4LC4

1.0LC1+0.4LC3+0.50LC2

1.0LC1+0.4LC4+0.50LC2

1.0LC1+0.60LC2

## 3.7 施加荷载

在 RFEM6.1 结构计算软件中，将上述荷载分别施加到对应杆件上，结构整体模型如下图 3.2 所示。恒荷载、活荷载加载如图 3.3 和图 3.4 所示。

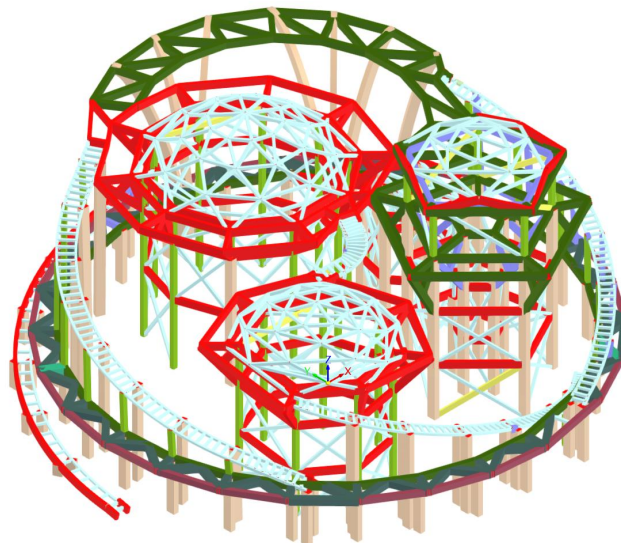


图 3.2 结构整体模型

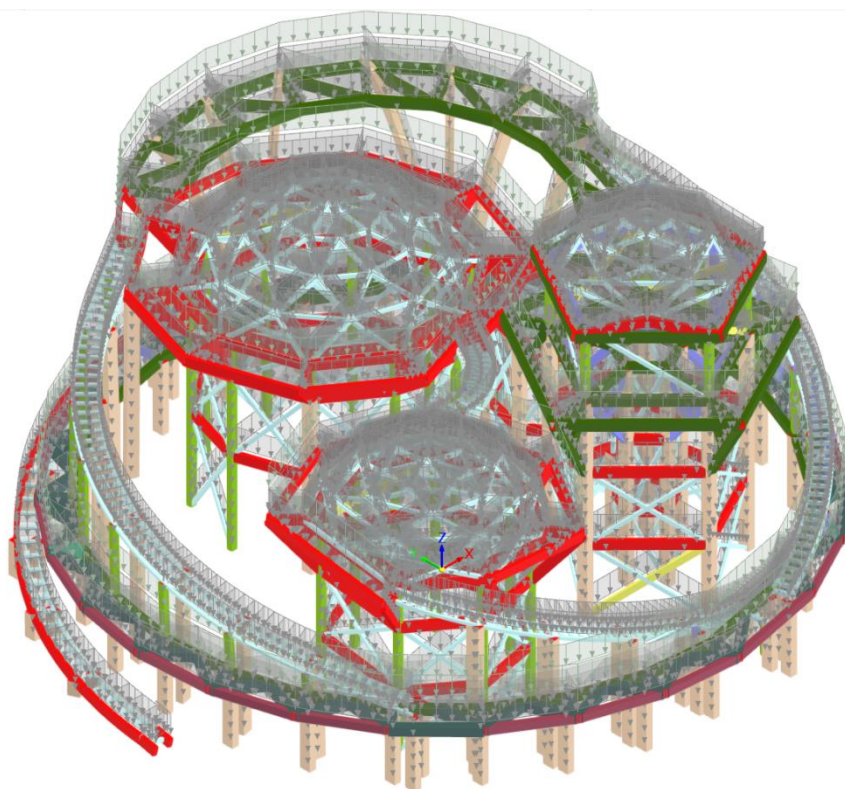


图 3.3恒荷载加载图

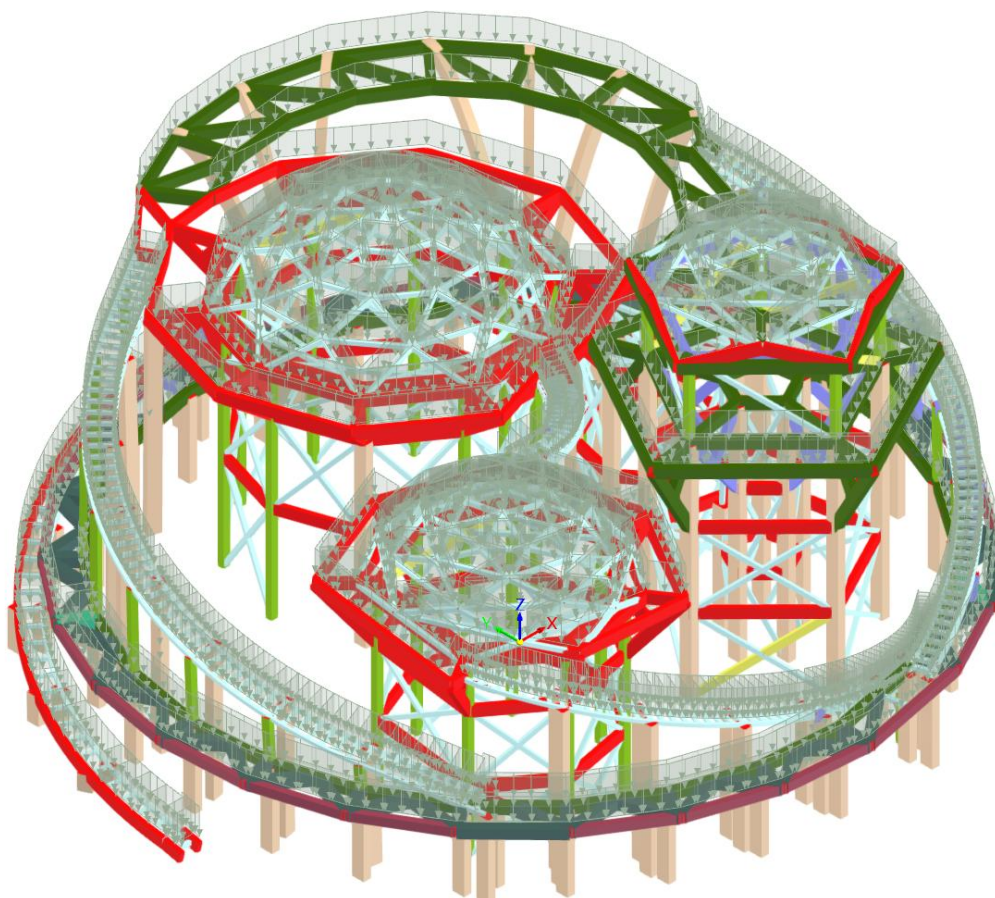


图 3.4活荷载加载图

### 3.8 构件内力分析

在 RFEM6.1 结构计算软件中，完成模型建立与荷载输入后，使用分析功能对结构再进行计算，得到各工况下各杆件的内力与弯矩数值。

根据内力结果，进行分析， $1.30LC1+1.50LC4+1.05LC2$  作用组合为最不利作用组合，考虑到该结构所受活载为  $0.50\text{ kN/m}^2$ ，场地基本风压为  $0.40\text{ kN/m}^2$ ，分析结果可信度较高。下面给出结构在这种工况下的主要内力分布以及弯矩图，如图 3.5-图 3.9 所示。

CO7 - 1.30 \* LC1 + 1.05 \* LC2 + 1.50 \* LC3

N [kN]

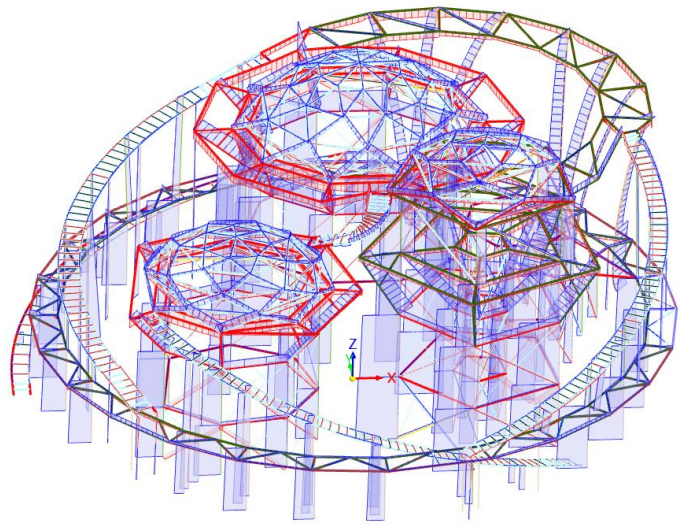


图 3.5轴力N分布图

CO7 - 1.30 \* LC1 + 1.05 \* LC2 + 1.50 \* LC3

V<sub>y</sub> [kN]

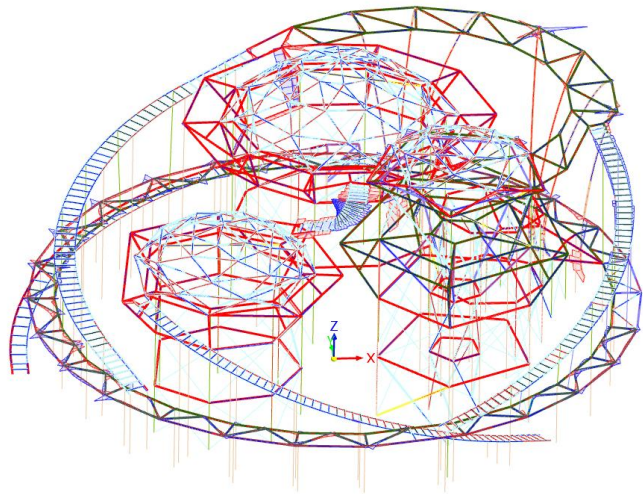
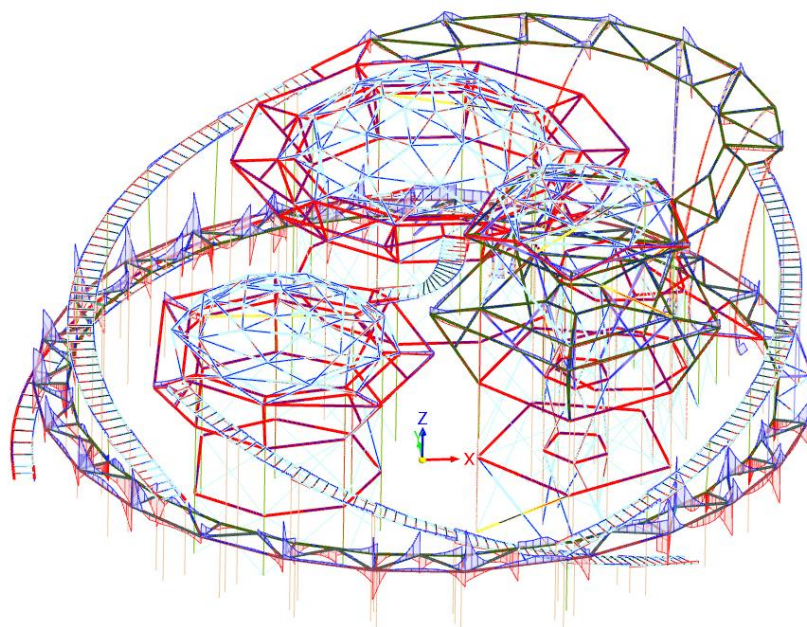
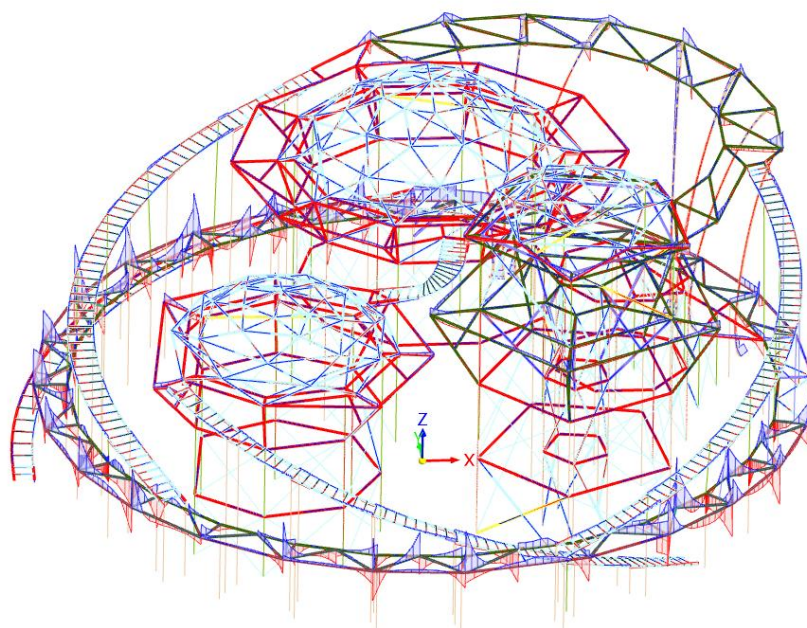


图 3.6剪力V<sub>y</sub>分布图

$CO7 - 1.30 * LC1 + 1.05 * LC2 + 1.50 * LC3$  $V_z$  [kN]图 3.7剪力 $V_z$ 分布图 $CO7 - 1.30 * LC1 + 1.05 * LC2 + 1.50 * LC3$  $V_z$  [kN]图 3.8弯矩 $M_y$ 分布图

$CO7 - 1.30 * LC1 + 1.05 * LC2 + 1.50 * LC3$

$M_z$  [kNm]

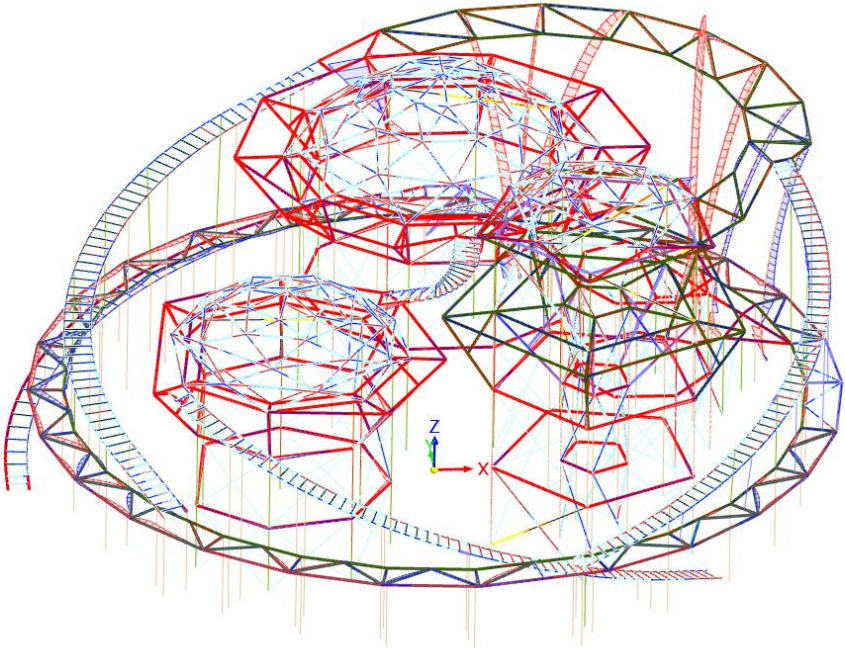


图 3.9弯矩Mz分布图

4 构件设计与验算

4.1 构件最大内力汇总

根据软件 RFEM6.1 的初步运行结果，获得杆件在 CO4 荷载工况的最大内力如表 4.1 所示。其中，N 为杆件轴力， $V_y$  为沿 y 轴的剪力， $V_z$  为沿 z 轴的剪力， $M_y$  为绕 y 轴的弯矩， $M_z$  为绕 z 轴的弯矩，杆件所受的扭矩均较小，暂不考虑。

表 4.1最大内力表

| 类型        | 杆件<br>编号 | 力 [kN]  |        |         | 弯矩[Knm] |       |
|-----------|----------|---------|--------|---------|---------|-------|
|           |          | N       | $V_y$  | $V_z$   | $M_y$   | $M_z$ |
| N 最大值     | 2220     | 122.30  | 4.69   | -24.23  | 12.27   | 0.85  |
| N 最小值     | 1410     | -351.89 | 0.00   | 0.00    | 0.00    | 0.00  |
| $V_y$ 最大值 | 1848     | -20.08  | 48.30  | -133.98 | 2.53    | 0.45  |
| $V_y$ 最小值 | 1851     | 2.64    | -76.05 | 81.40   | 0.83    | -2.79 |
| $V_z$ 最大值 | 252      | 3.07    | -14.80 | 413.16  | 4.05    | -0.60 |
| $V_z$ 最小值 | 288      | -56.92  | 1.20   | -512.72 | -109.90 | 0.03  |
| MT 最大值    | 217      | -15.09  | -3.63  | -96.10  | 2.24    | 4.37  |
| MT 最小值    | 230      | -10.34  | 1.99   | 301.56  | -0.76   | -0.25 |
| $M_y$ 最大值 | 230      | -11.61  | -0.12  | -11.27  | 255.10  | -0.79 |

|        |      |        |        |        |         |        |
|--------|------|--------|--------|--------|---------|--------|
| My 最小值 | 205  | -11.32 | -0.08  | 18.66  | -299.85 | 1.54   |
| Mz 最大值 | 1944 | -69.89 | 3.37   | -12.45 | 6.65    | 99.59  |
| Mz 最小值 | 1938 | 45.30  | -28.72 | 1.42   | 49.70   | -96.10 |

考虑到沿 x 轴的内力与绕 y 轴的弯矩较大，宜将 x 轴方向的截面尺寸增大，同时考虑到建筑跨度较大，应加大设计构件的截面高度（即 z 轴方向的截面尺寸）。

## 4.2 梁设计与验算

### 4.2.1 材料性能

梁材料树种选用对称异等组合胶合木，树种级别 SZ1，强度等级为 TC130，强度设计值与弹性模量见表 4.2。

| 材料基本属性单位（N/mm <sup>2</sup> ） |                     |         |
|------------------------------|---------------------|---------|
| 弹性模量                         | E                   | 14000.0 |
| 剪切模量                         | LC1                 | 1050.0  |
| 承压强度（横纹，全表面）                 | fc,90,total         | 3.000   |
| 承压强度（横纹，局部表面）                | fc,90,local         | 6.000   |
| 承压强度（横纹，垫板）                  | fc,90,bolster plate | 7.500   |
| 纵向抗剪承载力                      | fv                  | 2.200   |
| 顺纹抗拉承载力                      | ft                  | 20.000  |
| 顺纹抗压承载力                      | fc                  | 25.000  |
| 抗弯强度设计值                      | fm                  | 30.000  |

### 4.2.2 主体结构梁设计

4.2.2.1(1) 按照高度从底到高将三个展览室分为1、2、3号展览室，一层平台外侧梁截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{15.13 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{23.85 \text{ kN} \cdot 20250.00 \text{ cm}^3}{810000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.060 \\
 \eta &= 0.060 \leq 1 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_y \cdot S_z}{I_z \cdot h \cdot f_v} \\
 &= \frac{1.72 \text{ kN} \cdot 15187.50 \text{ cm}^3}{455625.00 \text{ cm}^4 \cdot 600.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.004 \\
 \eta &= 0.004 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2 \\
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 4.662 \text{ m} \\
 &= 4.662 \text{ m} \\
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{4.662 \text{ m}}{600.0 \text{ mm}} \\
 &= 7.77 \\
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(7.77)^2} \\
 &= 108.972 \text{ N/mm}^2 \\
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{108.972 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{108.972 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{108.972 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.972 \\
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{15.13 \text{ kN}}{0.972 \cdot 2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \quad \checkmark
 \end{aligned}$$

挠度验算:

正常使用极限状态SLS，挠度可忽略不计

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{11.61 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.001 \\
 \eta &= 0.001 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.2 (2) 一层平台中间梁

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{2.22 \text{ kN}}{400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 3.237 \text{ m} \\
 &= 3.237 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{3.237 \text{ m}}{200.0 \text{ mm}} \\
 &= 16.18
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(16.18)^2} \\
 &= 25.125 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{25.125 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{25.125 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{25.125 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.762
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{2.22 \text{ kN}}{0.762 \cdot 400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.003
 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
\beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
&= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
&= 0.76 \text{ mm/分钟} \\
T &= t \cdot \beta_e \\
&= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
&= 45.6 \text{ mm} \\
f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
&= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
&= 37.820 \text{ N/mm}^2 \\
\eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
&= \frac{1.70 \text{ kN}}{308.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
&= 0.001 \\
\eta &= 0.001 \leq 1 \checkmark
\end{aligned}$$

满足要求。

#### 4.2.2.3 (3) 一层平台内侧梁

截面强度验算：

$$\begin{aligned}
f_t &= f_{t,tab} \cdot k_{lt,f} \\
&= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
&= 20.000 \text{ N/mm}^2 \\
\eta &= \frac{N_t}{A_n \cdot f_t} \\
&= \frac{12.92 \text{ kN}}{1650.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
&= 0.004 \\
\eta &= 0.004 \leq 1 \checkmark
\end{aligned}$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{9.92 \text{ kN}}{1513.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.4 (4) 三层平台外侧梁

截面强度验算:

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{49.43 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.009 \\
 \eta &= 0.009 \leq 1 \checkmark
 \end{aligned}$$

抗火验算:

$$\begin{aligned}
\beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
&= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
&= 0.76 \text{ mm/分钟} \\
T &= t \cdot \beta_e \\
&= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
&= 45.6 \text{ mm} \\
f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
&= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
&= 36.720 \text{ N/mm}^2 \\
\eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
&= \frac{38.11 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
&= 0.004 \\
\eta &= 0.004 \leq 1 \quad \checkmark
\end{aligned}$$

满足要求。

#### 4.2.2.5 (5) 三层平台中间梁

截面强度验算:

$$\begin{aligned}
f_c &= f_{c,tab} \cdot k_{lt,f} \\
&= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
&= 25.000 \text{ N/mm}^2 \\
\eta &= \frac{N_c}{A_n \cdot f_c} \\
&= \frac{9.09 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
&= 0.001 \\
\eta &= 0.001 \leq 1 \quad \checkmark
\end{aligned}$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 3.440 \text{ m} \\
 &= 3.440 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{3.440 \text{ m}}{600.0 \text{ mm}} \\
 &= 5.73
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(5.73)^2} \\
 &= 200.174 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{200.174 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{200.174 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{200.174 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.986
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{9.09 \text{ kN}}{0.986 \cdot 2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

$$\begin{aligned}
 \eta &= \frac{M_y}{\varphi_{ly} \cdot W_{ny} \cdot f_{my}} \\
 &= \frac{16.64 \text{ kNm}}{0.961 \cdot 21125.00 \text{ cm}^3 \cdot 21.310 \text{ N/mm}^2} \\
 &= 0.038
 \end{aligned}$$

抗火验算：

$$\begin{aligned} f_v &= f_{v,tab} \cdot k_{lt,f} \\ &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\ &= 2.200 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\ &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\ &= 0.76 \text{ mm/分钟} \end{aligned}$$

$$\begin{aligned} T &= t \cdot \beta_e \\ &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\ &= 45.6 \text{ mm} \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned} \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\ &= \frac{17.70 \text{ kN} \cdot 17289.00 \text{ cm}^3}{639000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\ &= 0.048 \end{aligned}$$

$$\eta = 0.048 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.6 (6) 三层平台内侧梁

截面强度验算：

$$\begin{aligned} f_t &= f_{t,tab} \cdot k_{lt,f} \\ &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\ &= 20.000 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \eta &= \frac{N_t}{A_n \cdot f_t} \\ &= \frac{23.85 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\ &= 0.004 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{18.26 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002
 \end{aligned}$$

$$\eta = 0.002 \leq 1 \checkmark$$

满足要求。

#### 4.2.2.7 (7) 三层平台与楼梯连梁

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{49.15 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.007
 \end{aligned}$$

$$\eta = 0.007 \leq 1 \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 6.942 \text{ m} \\
 &= 6.942 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{6.942 \text{ m}}{600.0 \text{ mm}} \\
 &= 11.57
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(11.57)^2} \\
 &= 49.151 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{49.151 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{49.151 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{49.151 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.919
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{49.15 \text{ kN}}{0.919 \cdot 2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{37.79 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.004 \\
 \eta &= 0.004 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.8 (8) 1号展览室平台外侧梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{22.30 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.006 \\
 \eta &= 0.006 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{17.15 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.003
 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.9 (9) 1号展览室平台中部梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{32.56 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟}
 \end{aligned}$$

$$\begin{aligned}
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{25.05 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.004
 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.10 (10) 1号展览室平台内侧梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{11.06 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.003
 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{8.51 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \checkmark$$

满足要求。

#### 4.2.2.11 (11) 2号展览室平台外侧梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{17.94 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.005
 \end{aligned}$$

$$\eta = 0.005 \leq 1 \checkmark$$

抗火验算：

$$\begin{aligned}
\beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
&= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
&= 0.76 \text{ mm/分钟} \\
T &= t \cdot \beta_e \\
&= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
&= 45.6 \text{ mm} \\
f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
&= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
&= 36.720 \text{ N/mm}^2 \\
\eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
&= \frac{13.77 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
&= 0.002 \\
\eta &= 0.002 \leq 1 \quad \checkmark
\end{aligned}$$

## 4.2.2.12 (12) 2号展览室平台中间梁

截面强度验算:

$$\begin{aligned}
f_t &= f_{t,tab} \cdot k_{lt,f} \\
&= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
&= 20.000 \text{ N/mm}^2 \\
\eta &= \frac{N_t}{A_n \cdot f_t} \\
&= \frac{23.89 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
&= 0.006 \\
\eta &= 0.006 \leq 1 \quad \checkmark
\end{aligned}$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{18.37 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.003 \\
 \eta &= 0.003 \leq 1 \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.13 (13) 2号展览室平台内侧梁

截面强度验算:

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{32.39 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.008 \\
 \eta &= 0.008 \leq 1 \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{24.95 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.004 \\
 \eta &= 0.004 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.14 (14) 3号展览室平台外侧梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{10.14 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{2.06 \text{ kN} \cdot 20250.00 \text{ cm}^3}{810000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.005 \\
 \eta &= 0.005 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned} f_v &= f_{v,tab} \cdot k_{lt,f} \\ &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\ &= 2.200 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\ &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\ &= 0.76 \text{ mm/分钟} \end{aligned}$$

$$\begin{aligned} T &= t \cdot \beta_e \\ &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\ &= 45.6 \text{ mm} \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值,出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned} \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\ &= \frac{1.59 \text{ kN} \cdot 17289.00 \text{ cm}^3}{639000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\ &= 0.004 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.15 (15) 3号展览室平台中间梁

截面强度验算：

$$\begin{aligned} f_t &= f_{t,tab} \cdot k_{lt,f} \\ &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\ &= 20.000 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \eta &= \frac{N_t}{A_n \cdot f_t} \\ &= \frac{18.50 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\ &= 0.003 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

$$\begin{aligned} f_v &= f_{v,tab} \cdot k_{lt,f} \\ &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\ &= 2.200 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\ &= \frac{10.83 \text{ kN} \cdot 20250.00 \text{ cm}^3}{810000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\ &= 0.027 \end{aligned}$$

$$\eta = 0.027 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{14.23 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \checkmark
 \end{aligned}$$

#### 4.2.2.16 (16) 3号展览室平台内侧梁

截面强度验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{10.83 \text{ kN} \cdot 20250.00 \text{ cm}^3}{810000.00 \text{ cm}^4 \cdot 450.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.027 \\
 \eta &= 0.027 \leq 1 \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{14.23 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002
 \end{aligned}$$

$$\eta = 0.002 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.17 (17) 1号展览室柱间横梁

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{3.26 \text{ kN}}{400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.003
 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 2.550 \text{ m} \\
 &= 2.550 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{2.550 \text{ m}}{200.0 \text{ mm}} \\
 &= 12.75
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(12.75)^2} \\
 &= 40.492 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{40.492 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{40.492 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{40.492 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.891
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{3.26 \text{ kN}}{0.891 \cdot 400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.004
 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{2.50 \text{ kN}}{308.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.18 (18) 2号展览室柱间横梁

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{7.61 \text{ kN}}{400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008 \\
 \eta &= 0.008 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 3.105 \text{ m} \\
 &= 3.105 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{3.105 \text{ m}}{200.0 \text{ mm}} \\
 &= 15.52
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(15.52)^2} \\
 &= 27.302 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{0.9 f_c}} \\
 &= \frac{1 + \left( \frac{27.302 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{27.302 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{27.302 \text{ N/mm}^2}{0.9 \cdot 25.000 \text{ N/mm}^2}} \\
 &= 0.792
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{7.61 \text{ kN}}{0.792 \cdot 400.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.010
 \end{aligned}$$

$$\eta = 0.010 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{5.85 \text{ kN}}{308.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.005 \\
 \eta &= 0.005 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.19 (19) 3号展览室柱间横梁

截面强度验算：

$$\begin{aligned}
 f_t &= f_{t,tab} \cdot k_{lt,f} \\
 &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 20.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_t} \\
 &= \frac{2.65 \text{ kN}}{400.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\
 &= 0.003 \\
 \eta &= 0.003 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{2.04 \text{ kN}}{308.80 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002
 \end{aligned}$$

$$\eta = 0.002 \leq 1 \checkmark$$

满足要求。

#### 4.2.2.20 (20) 1号展览室屋顶处斜梁

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{5.17 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 7.182 \text{ m} \\
 &= 7.182 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{7.182 \text{ m}}{650.0 \text{ mm}} \\
 &= 11.05
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(11.05)^2} \\
 &= 53.902 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{53.902 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{53.902 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{53.902 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.930
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{5.17 \text{ kN}}{0.930 \cdot 1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟}
 \end{aligned}$$

$$\begin{aligned}
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

防火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{3.50 \text{ kN} \cdot 13698.70 \text{ cm}^3}{551967.00 \text{ cm}^4 \cdot 300.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.013
 \end{aligned}$$

$$\eta = 0.013 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.21 (21) 2号展览室屋顶处斜梁

截面强度验算:

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{3.07 \text{ kN} \cdot 15843.80 \text{ cm}^3}{686563.00 \text{ cm}^4 \cdot 300.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.011
 \end{aligned}$$

$$\eta = 0.011 \leq 1 \quad \checkmark$$

防火验算:

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟}
 \end{aligned}$$

$$\begin{aligned}
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{2.36 \text{ kN} \cdot 13698.70 \text{ cm}^3}{551967.00 \text{ cm}^4 \cdot 300.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.009
 \end{aligned}$$

$$\eta = 0.009 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.22 (22) 2号展览室屋顶处斜梁

截面强度验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{26.41 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.005
 \end{aligned}$$

$$\eta = 0.005 \leq 1 \quad \checkmark$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 7.557 \text{ m} \\
 &= 7.557 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{7.557 \text{ m}}{650.0 \text{ mm}} \\
 &= 11.63
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(11.63)^2} \\
 &= 48.681 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{0.9}} \\
 &= \frac{1 + \left( \frac{48.681 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{48.681 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{48.681 \text{ N/mm}^2}{0.9}} \\
 &= 0.918
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{26.41 \text{ kN}}{0.918 \cdot 1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.006
 \end{aligned}$$

$$\eta = 0.006 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{20.30 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.003 \\
 \eta &= 0.003 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.2.2.23 (23) 3号展览室屋顶处斜梁

截面强度验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{1.38 \text{ kN} \cdot 15843.80 \text{ cm}^3}{686563.00 \text{ cm}^4 \cdot 300.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.005 \\
 \eta &= 0.005 \leq 1 \quad \checkmark
 \end{aligned}$$

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_y \cdot S_z}{I_z \cdot h \cdot f_v} \\
 &= \frac{0.41 \text{ kN} \cdot 7312.50 \text{ cm}^3}{146250.00 \text{ cm}^4 \cdot 650.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.001 \\
 \eta &= 0.001 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火验算：

$$\begin{aligned} f_v &= f_{v,tab} \cdot k_{lt,f} \\ &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\ &= 2.200 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\ &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\ &= 0.76 \text{ mm/分钟} \end{aligned}$$

$$\begin{aligned} T &= t \cdot \beta_e \\ &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\ &= 45.6 \text{ mm} \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned} \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\ &= \frac{1.06 \text{ kN} \cdot 13698.70 \text{ cm}^3}{551967.00 \text{ cm}^4 \cdot 300.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\ &= 0.004 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.24 (24) 1号展览室平台处耦撑

截面强度验算：

$$\begin{aligned} f_c &= f_{c,tab} \cdot k_{lt,f} \\ &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\ &= 25.000 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \eta &= \frac{N_c}{A_n \cdot f_c} \\ &= \frac{44.90 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\ &= 0.009 \end{aligned}$$

$$\eta = 0.009 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 4.610 \text{ m} \\
 &= 4.610 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{4.610 \text{ m}}{650.0 \text{ mm}} \\
 &= 7.09
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(7.09)^2} \\
 &= 130.826 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{0.9 f_c}} \\
 &= \frac{1 + \left( \frac{130.826 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{130.826 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{130.826 \text{ N/mm}^2}{0.9 \cdot 25.000 \text{ N/mm}^2}} \\
 &= 0.978
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{44.90 \text{ kN}}{0.978 \cdot 1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.009
 \end{aligned}$$

$$\eta = 0.009 \leq 1 \quad \checkmark$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟}
 \end{aligned}$$

$$\begin{aligned}
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{34.54 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.005
 \end{aligned}$$

$$\eta = 0.005 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.25 (25) 2号展览室平台处耦撑

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{38.52 \text{ kN}}{1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 4.813 \text{ m} \\
 &= 4.813 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{4.813 \text{ m}}{650.0 \text{ mm}} \\
 &= 7.40
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(7.40)^2} \\
 &= 120.036 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{120.036 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{120.036 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{120.036 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.975
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{38.52 \text{ kN}}{0.975 \cdot 1950.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{29.63 \text{ kN}}{1813.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.004
 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

满足要求。

#### 4.2.2.26 (26) 3号展览室平台处耦撑

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{56.18 \text{ kN}}{2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 5.831 \text{ m} \\
 &= 5.831 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{5.831 \text{ m}}{600.0 \text{ mm}} \\
 &= 9.72
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(9.72)^2} \\
 &= 69.671 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{69.671 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{69.671 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{69.671 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.951
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{56.18 \text{ kN}}{0.951 \cdot 2700.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.009
 \end{aligned}$$

$$\eta = 0.009 \leq 1 \quad \checkmark$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{c,fi} &= f_{c,tab} \cdot k_{f_{c,fi}} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{43.21 \text{ kN}}{2494.80 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.005
 \end{aligned}$$

$$\eta = 0.005 \leq 1 \quad \checkmark$$

满足要求。

## 4.3 柱设计

柱子与梁相同材料，由两根200mm×450mm柱组合而成，间距为200mm，中间部分由垫块进行连接，每1.5m设置一个垫块。在设计计算时，将两根分支柱简化为一根柱子进行计算，简化后柱截面尺寸为400mm×450mm。

### 4.3.1.1 (1) 一层外侧柱

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{76.68 \text{ kN}}{4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z} &= k_{l,z} \cdot l_z \\
 &= 1.000 \cdot 5.000 \text{ m} \\
 &= 5.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z}/b &= \frac{l_{0,z}}{b} \\
 &= \frac{5.000 \text{ m}}{800.0 \text{ mm}} \\
 &= 6.25
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,z} &= 0.47 \cdot \frac{E}{(l_{0,z}/b)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(6.25)^2} \\
 &= 168.448 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_z &= \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,z}}{f_c}} \\
 &= \frac{1 + \left( \frac{168.448 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{168.448 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{168.448 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.983
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_z \cdot A_0 \cdot f_c} \\
 &= \frac{76.68 \text{ kN}}{0.983 \cdot 4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{c,fi} &= f_{ck,tab} \cdot k_{fc,fi} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{58.98 \text{ kN}}{3635.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.004
 \end{aligned}$$

$$\eta = 0.004 \leq 1 \quad \checkmark$$

满足要求。

#### 4.3.1.2 (2) 1号展览室柱

截面稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{108.62 \text{ kN}}{1800.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.024
 \end{aligned}$$

$$\eta = 0.024 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 12.000 \text{ m} \\
 &= 12.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{12.000 \text{ m}}{450.0 \text{ mm}} \\
 &= 26.67
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(26.67)^2} \\
 &= 9.253 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{9.253 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{9.253 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{9.253 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.351
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{108.62 \text{ kN}}{0.351 \cdot 1800.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.069
 \end{aligned}$$

$$\eta = 0.069 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 f_{c,fi} &= f_{ck,tab} \cdot k_{f_{c,fi}} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{83.55 \text{ kN}}{1617.60 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.014
 \end{aligned}$$

$$\eta = 0.014 \leq 1 \quad \checkmark$$

满足要求。

#### 4.3.1.3 (3) 2号展览室柱

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{148.94 \text{ kN}}{4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.015
 \end{aligned}$$

$$\eta = 0.015 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 12.000 \text{ m} \\
 &= 12.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{12.000 \text{ m}}{500.0 \text{ mm}} \\
 &= 24.00
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(24.00)^2} \\
 &= 11.424 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{11.424 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{11.424 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{11.424 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.425
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{148.94 \text{ kN}}{0.425 \cdot 4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.035
 \end{aligned}$$

$$\eta = 0.035 \leq 1 \quad \checkmark$$

抗火验算:

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{f_{c,fi}} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{114.57 \text{ kN}}{3635.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.008 \\
 \eta &= 0.008 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.3.1.4 (4) 3号展览室柱

截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{174.95 \text{ kN}}{4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.017 \\
 \eta &= 0.017 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z} &= k_{l,z} \cdot l_z \\
 &= 1.000 \cdot 15.000 \text{ m} \\
 &= 15.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z}/b &= \frac{l_{0,z}}{b} \\
 &= \frac{15.000 \text{ m}}{800.0 \text{ mm}} \\
 &= 18.75
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,z} &= 0.47 \cdot \frac{E}{(l_{0,z}/b)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(18.75)^2} \\
 &= 18.716 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_z &= \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,z}}{0.9 f_c}} \\
 &= \frac{1 + \left( \frac{18.716 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{18.716 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{18.716 \text{ N/mm}^2}{0.9 \cdot 25.000 \text{ N/mm}^2}} \\
 &= 0.637
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_z \cdot A_0 \cdot f_c} \\
 &= \frac{174.95 \text{ kN}}{0.637 \cdot 4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.027
 \end{aligned}$$

$$\eta = 0.027 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}\beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\ &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\ &= 0.76 \text{ mm/分钟}\end{aligned}$$

$$\begin{aligned}T &= t \cdot \beta_e \\ &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\ &= 45.6 \text{ mm}\end{aligned}$$

$$\begin{aligned}f_{c,fi} &= f_{c,tab} \cdot k_{f,fi} \\ &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\ &= 37.820 \text{ N/mm}^2\end{aligned}$$

$$\begin{aligned}\eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\ &= \frac{134.57 \text{ kN}}{3635.20 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\ &= 0.010\end{aligned}$$

$$\eta = 0.010 \leq 1 \quad \checkmark$$

满足要求。

#### 4.3.1.5 (5) 一层楼梯柱

始端截面强度验算：

$$\begin{aligned}f_c &= f_{c,tab} \cdot k_{lt,f} \\ &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\ &= 25.000 \text{ N/mm}^2\end{aligned}$$

$$\begin{aligned}\eta &= \frac{N_c}{A_n \cdot f_c} \\ &= \frac{10.09 \text{ kN}}{4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\ &= 0.001\end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

稳定性验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z} &= k_{l,z} \cdot l_z \\
 &= 1.000 \cdot 1.000 \text{ m} \\
 &= 1.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z}/b &= \frac{l_{0,z}}{b} \\
 &= \frac{1.000 \text{ m}}{800.0 \text{ mm}} \\
 &= 1.25
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,z} &= 0.47 \cdot \frac{E}{(l_{0,z}/b)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(1.25)^2} \\
 &= 4211.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_z &= \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,z}}{f_c}} \\
 &= \frac{1 + \left( \frac{4211.200 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{4211.200 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{4211.200 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.999
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_z \cdot A_0 \cdot f_c} \\
 &= \frac{10.09 \text{ kN}}{0.999 \cdot 4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟}
 \end{aligned}$$

$$\begin{aligned}
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{0.61 \text{ kN} \cdot 20647.90 \text{ cm}^3}{625495.00 \text{ cm}^4 \cdot 800.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

满足要求。

末端截面强度验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{10.09 \text{ kN}}{4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z} &= k_{l,z} \cdot l_z \\
 &= 1.000 \cdot 1.000 \text{ m} \\
 &= 1.000 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,z}/b &= \frac{l_{0,z}}{b} \\
 &= \frac{1.000 \text{ m}}{800.0 \text{ mm}} \\
 &= 1.25
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,z} &= 0.47 \cdot \frac{E}{(l_{0,z}/b)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(1.25)^2} \\
 &= 4211.200 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_z &= \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,z}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,z}}{0.9 f_c}} \\
 &= \frac{1 + \left( \frac{4211.200 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{4211.200 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{4211.200 \text{ N/mm}^2}{0.9 \cdot 25.000 \text{ N/mm}^2}} \\
 &= 0.999
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_z \cdot A_0 \cdot f_c} \\
 &= \frac{10.09 \text{ kN}}{0.999 \cdot 4000.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001
 \end{aligned}$$

$$\eta = 0.001 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{0.61 \text{ kN} \cdot 20647.90 \text{ cm}^3}{625495.00 \text{ cm}^4 \cdot 800.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.001 \\
 \eta &= 0.001 \leq 1 \quad \checkmark
 \end{aligned}$$

满足要求。

#### 4.3.1.6 (6) 一层至2号展览室楼梯柱

始端截面强度验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{36.59 \text{ kN}}{1800.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008 \\
 \eta &= 0.008 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 1.618 \text{ m} \\
 &= 1.618 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{1.618 \text{ m}}{450.0 \text{ mm}} \\
 &= 3.60
 \end{aligned}$$

$$\begin{aligned}
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(3.60)^2} \\
 &= 508.706 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \varphi_y &= \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{f_{cE,y}}{f_c} \right)}{1.8} \right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left( \frac{508.706 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} - \sqrt{\left( \frac{1 + \left( \frac{508.706 \text{ N/mm}^2}{25.000 \text{ N/mm}^2} \right)}{1.8} \right)^2 - \frac{508.706 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.995
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{36.59 \text{ kN}}{0.995 \cdot 1800.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.008
 \end{aligned}$$

$$\eta = 0.008 \leq 1 \quad \checkmark$$

抗火验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{c,fi} &= f_{ck,tab} \cdot k_{f_{c,fi}} \\
 &= 31.000 \text{ N/mm}^2 \cdot 1.22 \\
 &= 37.820 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_{c,fi}} \\
 &= \frac{27.96 \text{ kN}}{1617.60 \text{ cm}^2 \cdot 37.820 \text{ N/mm}^2} \\
 &= 0.005 \\
 \eta &= 0.005 \leq 1 \checkmark
 \end{aligned}$$

满足要求。

末端截面强度验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{12.05 \text{ kN} \cdot 10125.00 \text{ cm}^3}{303750.00 \text{ cm}^4 \cdot 400.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.046 \\
 \eta &= 0.046 \leq 1 \checkmark
 \end{aligned}$$

稳定性计算：

$$\begin{aligned}
 k_v &= \left[ \left( \frac{130}{b} \right) \cdot \left( \frac{305}{h} \right) \cdot \left( \frac{6400}{L} \right) \right]^{\frac{1}{c}} \\
 &= \left[ \left( \frac{130}{400.0 \text{ mm}} \right) \cdot \left( \frac{305}{450.0 \text{ mm}} \right) \cdot \left( \frac{6400}{8.509 \text{ m}} \right) \right]^{\frac{1}{10.00}} \\
 &= 0.84
 \end{aligned}$$

$$\begin{aligned}
 f_{m,y} &= f_{my,tab} \cdot k_v \cdot k_{lt,f} \cdot k_{dim} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.84 \cdot 1.00 \cdot 1.15 \\
 &= 28.823 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f_{m,z} &= f_{mz,tab} \cdot k_{sg,f} \cdot k_{dim} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.70 \cdot 1.15 \cdot 1.00 \\
 &= 24.150 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f'_{m,y} &= f_{my,tab} \cdot k_{dim} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 1.15 \cdot 1.00 \\
 &= 34.500 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f'_{m,z} &= f_{mz,tab} \cdot k_{sg,f} \cdot k_{dim} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.70 \cdot 1.15 \cdot 1.00 \\
 &= 24.150 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{e,y} &= k_{ltb} \cdot l_u \\
 &= 1.000 \cdot 9.521 \text{ m} \\
 &= 9.521 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \lambda_y &= \sqrt{\frac{l_{e,y} \cdot h}{(b)^2}} \\
 &= \sqrt{\frac{9.521 \text{ m} \cdot 0.45}{(0.4)^2}} \\
 &= 5.175
 \end{aligned}$$

$$\begin{aligned}
 f_{mE,y} &= 0.67 \cdot \frac{E}{(\lambda_y)^2} \\
 &= 0.67 \cdot \frac{14000.000 \text{ N/mm}^2}{(5.175)^2} \\
 &= 350.279 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 \eta &= \frac{M_y}{W_{ny} \cdot f_{m,y}} + \frac{M_z}{W_{nz} \cdot f_{m,z} \cdot \left[ 1 - \left( \frac{M_y}{W_{ny} \cdot f_{mE,y}} \right)^2 \right]} \\
 &= \frac{104.12 \text{ kNm}}{13500.00 \text{ cm}^3 \cdot 28.823 \text{ N/mm}^2} + \frac{12000.00 \text{ cm}^3 \cdot 24.150 \text{ N}}{12000.00 \text{ cm}^3 \cdot 24.150 \text{ N}} \\
 &= 0.525 \\
 \eta &= 0.525 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火性验算：

$$\begin{aligned}
 f_v &= f_{v,tab} \cdot k_{lt,f} \\
 &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\
 &= 2.200 \text{ N/mm}^2 \\
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm}
 \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值, 出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned}
 \eta &= \frac{V_z \cdot S_y}{I_y \cdot b \cdot f_v} \\
 &= \frac{9.26 \text{ kN} \cdot 8176.97 \text{ cm}^3}{220451.00 \text{ cm}^4 \cdot 400.0 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\
 &= 0.039 \\
 \eta &= 0.039 \leq 1 \quad \checkmark
 \end{aligned}$$

#### 4.3.1.7 (7) 一层至3号展览室楼梯柱

始端截面强度验算：

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 \eta &= \frac{N_c}{A_n \cdot f_c} \\
 &= \frac{5.18 \text{ kN}}{1650.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001 \\
 \eta &= 0.001 \leq 1 \quad \checkmark
 \end{aligned}$$

稳定性验算:

$$\begin{aligned}
 f_c &= f_{c,tab} \cdot k_{lt,f} \\
 &= 25.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 25.000 \text{ N/mm}^2 \\
 E &= E_{k,tab} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2 \\
 l_{0,y} &= k_{l,y} \cdot l_y \\
 &= 1.000 \cdot 1.846 \text{ m} \\
 &= 1.846 \text{ m} \\
 l_{0,y}/h &= \frac{l_{0,y}}{h} \\
 &= \frac{1.846 \text{ m}}{550.0 \text{ mm}} \\
 &= 3.36 \\
 f_{cE,y} &= 0.47 \cdot \frac{E}{(l_{0,y}/h)^2} \\
 &= 0.47 \cdot \frac{14000.000 \text{ N/mm}^2}{(3.36)^2} \\
 &= 584.148 \text{ N/mm}^2 \\
 \varphi_y &= \frac{1 + \left(\frac{f_{cE,y}}{f_c}\right)}{1.8} - \sqrt{\left(\frac{1 + \left(\frac{f_{cE,y}}{f_c}\right)}{1.8}\right)^2 - \frac{f_{cE,y}}{f_c}} \\
 &= \frac{1 + \left(\frac{584.148 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}\right)}{1.8} - \sqrt{\left(\frac{1 + \left(\frac{584.148 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}\right)}{1.8}\right)^2 - \frac{584.148 \text{ N/mm}^2}{25.000 \text{ N/mm}^2}} \\
 &= 0.996 \\
 \eta &= \frac{N_c}{\varphi_y \cdot A_0 \cdot f_c} \\
 &= \frac{5.18 \text{ kN}}{0.996 \cdot 1650.00 \text{ cm}^2 \cdot 25.000 \text{ N/mm}^2} \\
 &= 0.001 \\
 \eta &= 0.001 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火性验算:

$$\begin{aligned} f_v &= f_{v,tab} \cdot k_{lt,f} \\ &= 2.200 \text{ N/mm}^2 \cdot 1.00 \\ &= 2.200 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\ &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\ &= 0.76 \text{ mm/分钟} \end{aligned}$$

$$\begin{aligned} T &= t \cdot \beta_e \\ &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\ &= 45.6 \text{ mm} \end{aligned}$$

抗火设计时由于规范未给出抗剪强度平均值,出于更加保守考虑采用抗剪强度设计值  $f_v$  进行计算。

$$\begin{aligned} \eta &= \frac{V_y \cdot S_z}{I_z \cdot h \cdot f_v} \\ &= \frac{0.60 \text{ kN} \cdot 5674.50 \text{ cm}^3}{113490.00 \text{ cm}^4 \cdot 504.4 \text{ mm} \cdot 2.200 \text{ N/mm}^2} \\ &= 0.003 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

末端截面强度验算:

$$\begin{aligned} f_t &= f_{t,tab} \cdot k_{lt,f} \\ &= 20.000 \text{ N/mm}^2 \cdot 1.00 \\ &= 20.000 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \eta &= \frac{N_t}{A_n \cdot f_t} \\ &= \frac{11.03 \text{ kN}}{1650.00 \text{ cm}^2 \cdot 20.000 \text{ N/mm}^2} \\ &= 0.003 \end{aligned}$$

$$\eta = 0.003 \leq 1 \quad \checkmark$$

稳定性验算:

$$\begin{aligned}
 k_v &= \left[ \left( \frac{130}{b} \right) \cdot \left( \frac{305}{h} \right) \cdot \left( \frac{6400}{L} \right) \right]^{\frac{1}{c}} \\
 &= \left[ \left( \frac{130}{300.0 \text{ mm}} \right) \cdot \left( \frac{305}{550.0 \text{ mm}} \right) \cdot \left( \frac{6400}{8.956 \text{ m}} \right) \right]^{\frac{1}{10.00}} \\
 &= 0.84
 \end{aligned}$$

$$\begin{aligned}
 f_{m,y} &= f_{m,y,\text{tab}} \cdot k_v \cdot k_{lt,f} \cdot k_{\text{dim}} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.84 \cdot 1.00 \cdot 1.10 \\
 &= 27.669 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f_{m,z} &= f_{m,z,\text{tab}} \cdot k_{sg,f} \cdot k_{\text{dim}} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.70 \cdot 1.10 \cdot 1.00 \\
 &= 23.100 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f'_{m,y} &= f_{m,y,\text{tab}} \cdot k_{\text{dim}} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 1.10 \cdot 1.00 \\
 &= 33.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 f'_{m,z} &= f_{m,z,\text{tab}} \cdot k_{sg,f} \cdot k_{\text{dim}} \cdot k_{lt,f} \\
 &= 30.000 \text{ N/mm}^2 \cdot 0.70 \cdot 1.10 \cdot 1.00 \\
 &= 23.100 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 E &= E_{k,\text{tab}} \cdot k_{lt,E} \\
 &= 14000.000 \text{ N/mm}^2 \cdot 1.00 \\
 &= 14000.000 \text{ N/mm}^2
 \end{aligned}$$

$$\begin{aligned}
 l_{e,y} &= k_{ltb} \cdot l_u \\
 &= 1.000 \cdot 9.010 \text{ m} \\
 &= 9.010 \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 \lambda_y &= \sqrt{\frac{l_{e,y} \cdot h}{(b)^2}} \\
 &= \sqrt{\frac{9.010 \text{ m} \cdot 0.55}{(0.3)^2}} \\
 &= 7.420
 \end{aligned}$$

$$\begin{aligned}
 f_{mE,y} &= 0.67 \cdot \frac{E}{(\lambda_y)^2} \\
 &= 0.67 \cdot \frac{14000.000 \text{ N/mm}^2}{(7.420)^2} \\
 &= 170.352 \text{ N/mm}^2
 \end{aligned}$$

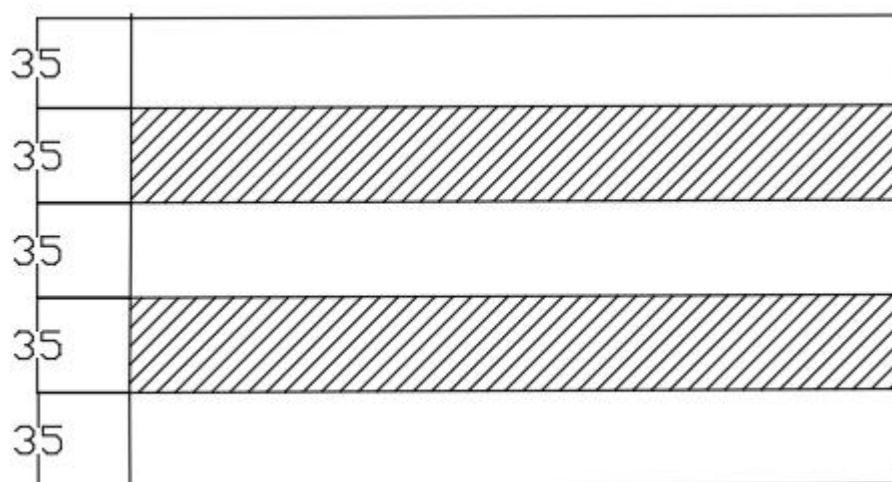
$$\begin{aligned}
 \eta &= \frac{M_y}{W_{ny} \cdot f_{m,y}} + \frac{M_z}{W_{nz} \cdot f_{m,z} \cdot \left[ 1 - \left( \frac{M_y}{W_{ny} \cdot f_{mE,y}} \right)^2 \right]} \\
 &= \frac{14.96 \text{ kNm}}{15125.00 \text{ cm}^3 \cdot 27.669 \text{ N/mm}^2} + \frac{8250.00 \text{ cm}^3 \cdot 23.100 \text{ N/mm}^2}{8250.00 \text{ cm}^3 \cdot 23.100 \text{ N/mm}^2} \\
 &= 0.085 \\
 \eta &= 0.085 \leq 1 \quad \checkmark
 \end{aligned}$$

抗火性验算：

$$\begin{aligned}
 \beta_e &= 1.2 \cdot \frac{\beta_n}{(t)^{0.187}} \\
 &= 1.2 \cdot \frac{0.63 \text{ mm/分钟}}{(1.00 \text{ 小时})^{0.187}} \\
 &= 0.76 \text{ mm/分钟} \\
 T &= t \cdot \beta_e \\
 &= 1.00 \text{ 小时} \cdot 0.76 \text{ mm/分钟} \\
 &= 45.6 \text{ mm} \\
 f_{t,fi} &= f_{tk,tab} \cdot k_{ft,fi} \\
 &= 27.000 \text{ N/mm}^2 \cdot 1.36 \\
 &= 36.720 \text{ N/mm}^2 \\
 \eta &= \frac{N_t}{A_n \cdot f_{t,fi}} \\
 &= \frac{8.46 \text{ kN}}{1513.20 \text{ cm}^2 \cdot 36.720 \text{ N/mm}^2} \\
 &= 0.002 \\
 \eta &= 0.002 \leq 1 \quad \checkmark
 \end{aligned}$$

## 5 楼板设计

楼板采用CLT材料，厚度为175mm，5层单板组成，宽度为0.6m，长度为7.5m，因此不利情况为楼板简支于主梁上，对其进行验算。



### 5.1 材料性能

本工程中CLT使用的木材为进口北美地区规格材云杉-松-冷杉类，材质等级为II<sub>c</sub>级，截面最大尺寸285mm，抗弯强度设计值 $f_m$ 为9.8 N/mm<sup>2</sup>，顺纹抗压强度设计值 $f_c$ 为11.5 N/mm<sup>2</sup>，顺纹抗拉强度设计值 $f_t$ 为4.0 N/mm<sup>2</sup>，顺纹抗剪强度设计值 $f_v$ 为1.4 N/mm<sup>2</sup>，横纹承压强度设计值 $f_{c,90}$ 为4.9 N/mm<sup>2</sup>，弹性模量 $E$ 为10000 N/mm<sup>2</sup>。

根据《木结构设计标准》LC1B50005-2017，CLT抗弯强度设计值为表层木材强度应乘以组合系数 $K_c$ ，见下式。并且，组合系数 $K_c$ 不应大于1.2。

$$K_c = 1 + 0.02n$$

式中， $n$ —最外侧层板并排布置的层板数量。

正交胶合木构件的有效抗弯刚度（ $EI$ ）应按下列公式计算：

$$(EI) = \sum_{i=1}^{n_i} (E_i I_i + E_i A_i e_i^2)^n$$

$$I_i = \frac{bt_i^3}{12}$$

$$A_i = bt_i$$

式中：

$E$ -- 参加计算的第  $i$  层顺纹层板的弹性模量(N/mm<sup>2</sup>);

$I_i$ --参加计算的第  $i$  层顺纹层板的截面惯性矩(mm<sup>4</sup>);

$A_i$  --参加计算的第  $i$  层顺纹层板的截面面积  $bt_i$ (mm<sup>2</sup>);

$b$ --构件的截面宽度(mm);

$t_i$ --参加计算的第*i*层顺纹层板的截面高度(mm);

$n_i$ -- 参加计算的顺纹层板的层数;

$e_i$ --参加计算的第*i*层顺纹层板的重心至截面重心的距离

根据以上规定, CLT力学性能指标计算为 $f_m=9.8 \times 1=9.8 \text{ N/mm}^2$ ,  $EI=1.77 \times 10^{12} \text{ N} \cdot \text{mm}^2$ 。

## 5.2 荷载组合

(1) 恒载:

7厚实木复合木地板 7.0kN/m<sup>3</sup>

175mm厚正交胶合木板 7.0kN/m<sup>3</sup>

(2) 活载:

荷载取值参照办公楼活荷载 2kN/m<sup>2</sup>

自重线荷载:  $0.7 \times 9.8 \times 0.175 \times 0.6 = 0.72 \text{ kN/m}$ ;

木地板自重产生的线荷载:  $0.7 \times 9.8 \times 0.007 \times 0.4 = 0.019 \text{ kN/m}$ ;

活载:  $3 \times 0.4 = 1.2 \text{ kN/m}$ 。

简支板跨中最大弯矩标准值为:

$$M_{\max} = [(0.48 + 0.019) \times 1.3 + 1.2 \times 1.5] \times 7.5 \times 7.5 / 2 - [(0.48 + 0.019 + 0.0012) \times 1.3 + 0.8 \times 1.5] \times 3.75 \times 3.75 / 2 = 51.65 \text{ kN} \cdot \text{m}$$

## 5.3 设计与验算

### 5.3.1 强度验算

当CLT受弯构件的跨度大于构件截面高度 $h$ 的10倍时, 构件的受弯承载能力应按下式验算:

$$\pm \frac{ME_I h}{2(EI)} \leq f_m$$

式中:

$E_i$ --最外侧顺纹层板的弹性模量(N/mm<sup>2</sup>);

$f_m$ --最外侧层板的抗弯强度设计值(N/mm<sup>2</sup>);

$M$ --受弯构件弯矩设计值(N.mm);

$(EI)$ --构件的有效抗弯刚度(N.mm);

$h$ --构件的截面高度(mm)。

计算可得 $f=3.98 \text{ MPa} < 0.9f_m=8.82 \text{ MPa}$  验算合格。

楼上活荷载为 $3 \text{ kN/m}^2$ , 楼板面积为 $2 \text{ m} \times 5 \text{ m}$ , 总荷载为 $P=3 \times 2 \times 5=30 \text{ kN}$

剪应力计算公式:

$$\tau = \frac{3V}{2bd}$$

剪力  $V=P/2=15\text{kN}$

因此,

$$\tau = \frac{3V}{2bd} = \frac{3 \times 15}{2 \times 0.4 \times 0.175} = 0.321\text{N/mm}^2$$
$$\tau = 0.321\text{N/mm}^2 < 1.4\text{N/mm}$$

### 5.3.2 挠度检验

CLT受弯构件的弯曲挠度按下式计算:

$$W = \frac{5ql^4}{384(EI)}$$

$W_{\max}=5 \times 5.17 \times 10^7 \times 5000^2 / (48 \times 1.77 \times 10^{12}) = 7.607\text{mm} < l/250 = 5000/250 = 20\text{ mm}$  验算合格。

因此, 175mm厚的CLT楼板在强度、挠度和滚动剪切方面均能满足稳定性和强度要求。

## 6 节点设计与验算

### 6.1 梁端节点计算

梁端头均采用M16对穿螺栓连接，连接方式均采用钢填板，连接板采用10mm厚Q235B镀锌铁板，螺栓采用8.8级普通螺栓；

每个销的每个剪切面承载力设计值计算： $Z = k_{min} t_m d f_{es}$

较薄构件厚度 $t_s=10\text{mm}$ ；较厚构件厚度 $t_m=150\text{mm}$ ；销轴类紧固件直径 $d=16\text{mm}$ 。

根据木结构设计规范，紧固件在钢材上的销槽承压强度 $f_{es}$ 应按现行国家标准《钢结构设计规范》LC1B50017规定的螺栓连接的构件销槽承压强度设计值的1.1倍计算

$$f_{es} = 160\text{MPa} \times 1.1 = 176\text{MPa}$$

计算时较厚构件销槽承压强度值 $f_{em}$ 取为销轴类紧固件销槽横纹承压强度，根据《木结构设计标准》（LC1B50005-2017），全干相对密度取0.42。

$$f_{em} = f_{e,90} = \frac{212G^{1.45}}{\sqrt{d}} = 32.34\text{N/mm}^2$$

$$\text{则 } R_e = \frac{f_{em}}{f_{es}} = 0.1837, R_t = \frac{t_m}{t_s} = \frac{150}{10} = 15$$

(1) 有效长度系数计算

最小有效长度系数计算： $k_{min} = \min [k_1, k_2, k_3, k_4]$

屈服模式I时，

$$k_I = \frac{R_e R_t}{\gamma_I} = 0.2756$$

屈服模式II时，

$$k_{sII} = \frac{\sqrt{R_e + 2R_e^2(1 + R_t + R_t^2) + R_t^2 R_e^3 - R_e(1 + R_t)}}{1 + R_e}$$

$$k_{II} = \frac{k_{sII}}{\gamma_{II}} = 0.5919$$

屈服模式III时， $k_{ep}$ 取1.0，销轴类紧固件屈服强度标准值 $f_{yk}$ 取235 N/mm<sup>2</sup>

$$k_{III m} = \frac{R_t R_e}{1 + 2R_e} \left[ \sqrt{2(1 + R_e) + \frac{1.647(1 + 2R_e)k_{ep}f_{yk}d^2}{3R_e R_t^2 f_{es} t_s^2}} - 1 \right]$$

$$k_{III m} = \frac{k_{III m}}{\gamma_{III}} = 0.5816$$

屈服模式III<sub>s</sub>时，

$$k_{III s} = \frac{R_e}{2 + R_e} \left[ \sqrt{\frac{2(1 + R_e)}{R_e} + \frac{1.647(2 + R_e)k_{ep}f_{yk}d^2}{3R_e R_t^2 f_{es} t_s^2}} - 1 \right]$$

$$k_{III} = \frac{k_{III s}}{\gamma_{III}} = 0.2756$$

屈服模式IV时，

$$k_{IVs} = \frac{d}{t_s} \sqrt{\frac{1.647 R_e k_{ep} f_{yk}}{3(1+R_e) f_{es}}}$$

$$k_{IV} = \frac{k_{IVs}}{\gamma_{IV}} = 0.3470$$

## (2) 承载力计算

螺栓受剪承载力计算，依据《钢结构设计规范》（LC1B/50017-2017），在普通螺栓或铆钉抗剪连接中，每个螺栓的承载力设计值应取受剪和承压承载力设计值中的较小者。受剪和承压承载力设计值应分别按下式计算。

普通螺栓：

$$N_v^b = n_v \frac{\pi d^2}{4} f_v^b$$

铆钉：

$$N_v^r = n_v \frac{\pi d_0^2}{4} f_v^r$$

普通螺栓：

$$N_c^b = d \sum t f_c^b$$

铆钉：

$$N_c^r = d_0 \sum t f_c^r$$

式中，

$n_v$ ——受剪面数目；

$d$ ——螺杆直径(mm)；

$d_0$ ——铆钉孔直径(mm)；

$\sum t$ ——在不同受力方向中一个受力方向承压构件总厚度的较小值(mm)；

$f_{bv}$ 、 $f_{bc}$ ——螺栓的抗剪和承压强度设计值(N/mm<sup>2</sup>)；

$f_{rv}$ 、 $f_{rc}$ ——铆钉的抗剪和承压强度设计值(N/mm<sup>2</sup>)。

螺栓的剪切强度：Q235钢材的抗剪强度约为210 MPa，

螺栓的截面积：

$$A = \frac{\pi d^2}{4} = 200.96 \text{ mm}^2$$

螺栓的单面剪切承载力：

$$F = 210 \text{ MPa} \times 200.96 \text{ mm}^2 = 42.2 \text{ kN}$$

螺栓材料本身的承载力远超木材的承载力，所以这里重点考虑木材的承载力。该连接为钢填板，故只需考虑屈服模式Is、IIIs与IV，在不考虑销屈服情况下 $K_{\min}=0.2756$

单个销的每个剪面承载力参考设计值：

$$Z = k_{min} t_s d f_{es} = 0.2756 \times 10 \times 16 \times 176 = 7.76 kN$$

每个剪面的承载力设计值:

$$Z_d = C_m C_n C_t k_g Z = 1 \times 1 \times 1 \times 1 \times 7.76 = 7.76 kN$$

每根螺栓与梁端产生两个剪力面, 因此一根螺栓在梁端的承载力为  $7.76 \times 2 = 15.52 kN$ 。

## 6.2 柱端节点计算

柱端头采用8.8级M16对穿螺栓连接, 每根螺栓产生一个顺纹单剪面。

每个销的每个剪面承载力设计值计算:  $Z = k_{min} t_m d f_{es}$

边部构件厚度  $t_s = 20 mm$ ; 中部构件厚度  $t_m = 240 mm$ ; 销轴类紧固件直径  $d = 16 mm$ 。

根据木结构设计规范, 紧固件在钢材上的销槽承压强度  $f_{es}$  应按现行国家标准《钢结构设计规范》LC1B50017规定的螺栓连接的构件销槽承压强度设计值的1.1倍计算

$$f_{es} = 160 MPa \times 1.1 = 176 MPa$$

计算时较厚构件销槽承压强度值  $f_{em}$  取为销轴类紧固件销槽横纹承压强度, 全干相对密度根据《木结构设计标准》(LC1B50005-2017) 取0.42。

$$f_{em} = f_{e,0} = 77 G = 77 \times 0.42 = 32.34 N/mm^2$$

$$\text{则 } R_e = \frac{f_{em}}{f_{es}} = 0.1326, R_t = \frac{t_m}{t_s} = \frac{240}{20} = 12$$

(1) 有效长度系数计算

最小有效长度系数计算:  $k_{min} = \min [k_1, k_2, k_3, k_4]$

屈服模式I时,

$$k_1 = \frac{R_e R_t}{\gamma_1} = 0.1989$$

屈服模式II时,

$$k_{sII} = \frac{\sqrt{R_e + 2R_e^2(1 + R_t + R_t^2) + R_t^2 R_e^3 - R_e(1 + R_t)}}{1 + R_e}$$

$$k_{II} = \frac{k_{sII}}{\gamma_{II}} = 0.4982$$

屈服模式III时,  $k_{ep}$  取1.0, 销轴类紧固件屈服强度标准值  $f_{yk}$  取  $235 N/mm^2$

$$k_{III m} = \frac{R_t R_e}{1 + 2R_e} \left[ \sqrt{2(1 + R_e) + \frac{1.647(1 + 2R_e) k_{ep} f_{yk} d^2}{3R_e R_t^2 f_{es} t_s^2}} - 1 \right]$$

$$k_{III m} = \frac{k_{III m}}{\gamma_{III}} = 0.2795$$

屈服模式III<sub>s</sub>时,

$$k_{III s} = \frac{R_e}{2 + R_e} \left[ \sqrt{\frac{2(1 + R_e)}{R_e} + \frac{1.647(2 + R_e) k_{ep} f_{yk} d^2}{3R_e R_t^2 f_{es} t_s^2}} - 1 \right]$$

$$k_{III} = \frac{k_{IIIs}}{\gamma_{III}} = 0.1989$$

屈服模式IV时,

$$k_{IVs} = \frac{d}{t_s} \sqrt{\frac{1.647 R_e k_{ep} f_{yk}}{3(1+R_e) f_{es}}}$$

$$k_{IV} = \frac{k_{IVs}}{\gamma_{IV}} = 0.2871$$

## (2) 承载力计算

柱端为钢夹板的单剪连接只需考虑屈服模式Is、IIIs以及IV，在不考虑螺栓屈服条件下，则 $K_{min}=0.1989$ 。

单个销的每个剪面承载力参考设计值：

$$Z = k_{min} t_s d f_{es} = 0.1989 \times 20 \times 16 \times 176 = 11.20 \text{ kN}$$

每个剪面的承载力设计值：

$$Z_d = C_m C_n C_t k_g Z = 1 \times 1 \times 1 \times 1 \times 11.20 = 11.20 \text{ kN}$$

每根螺栓与柱端产生一个剪力面，因此一根螺栓在柱端的承载力为11.20kN。

## 6.3 节点设计

### 6.3.1 I号节点螺栓设计

#### (1) 恒载：

屋面自重： $7 \times 0.175 \times 7 \times 3 = 25.725 \text{ kN}$

梁自重： $7 \text{ kN/m}^3 \times 0.45 \times 0.6 \times 5 \times 3 = 28.35 \text{ kN}$

荷载组合：1.3恒载+1.5活载

柱端所受总剪力：62.79 kN

I号节点设计图如下。

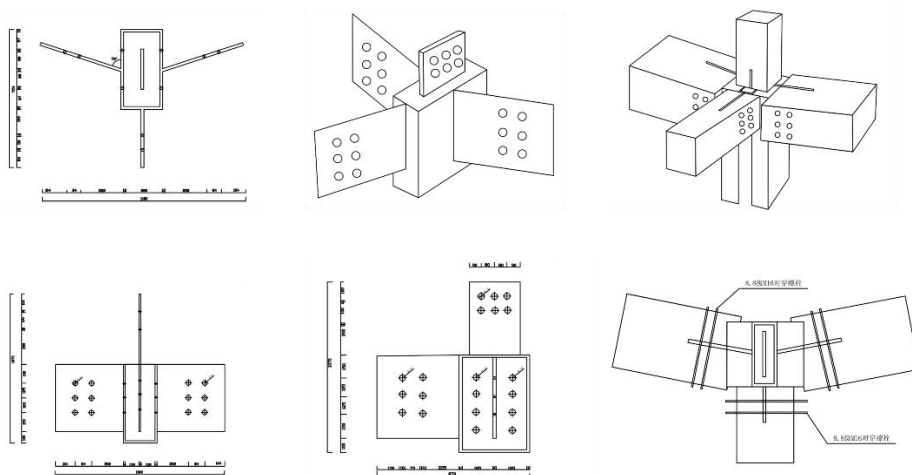


图 6.1 I号节点设计图

### 6.3.2 II号节点螺栓设计

(1) 恒载:

屋面自重:  $7 \times 0.175 \times 7 \times 3 = 25.725 \text{ kN}$

梁自重:  $7 \text{ kN/m}^3 \times 0.45 \times 0.6 \times 5 \times 2 = 18.9 \text{ kN}$

荷载组合: 1.3恒载+1.5活载

柱端所受总剪力: 72.19 kN

II号节点设计图如下。

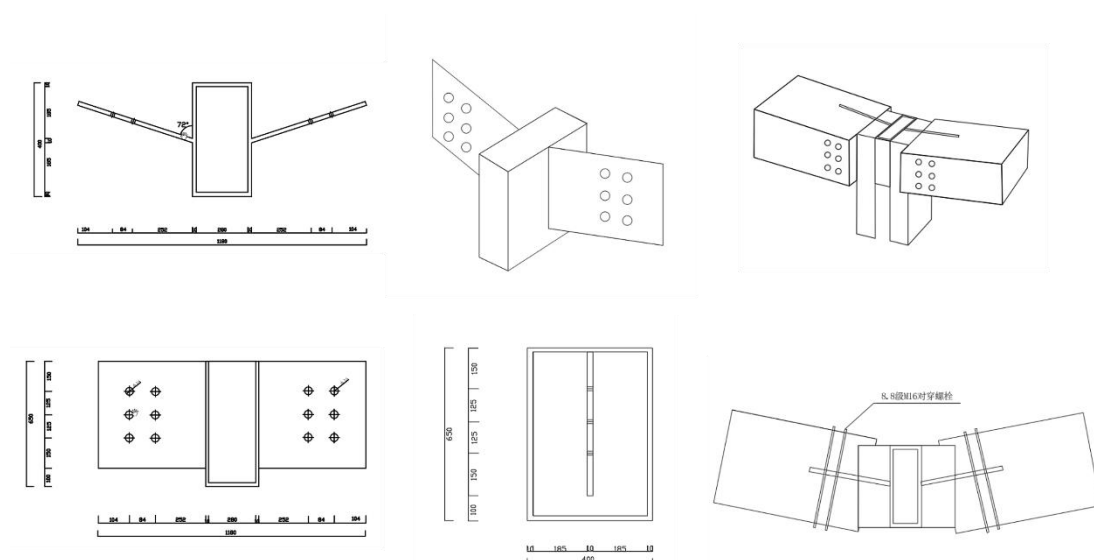


图 6.2 II号节点设计图

### 6.3.3 III号节点螺栓设计

(1) 恒载:

屋面自重:  $7 \times 0.175 \times 7 \times 3 = 25.725 \text{ kN}$

梁自重:  $7 \text{ kN/m}^3 \times (0.6 \times 0.45 \times 7 \times 2 + 0.6 \times 0.45 \times 2) = 17.01 \text{ kN}$

荷载组合: 1.3恒载+1.5活载

柱端所受总剪力: 30.85 kN

III号节点设计图如下。

节点详图III

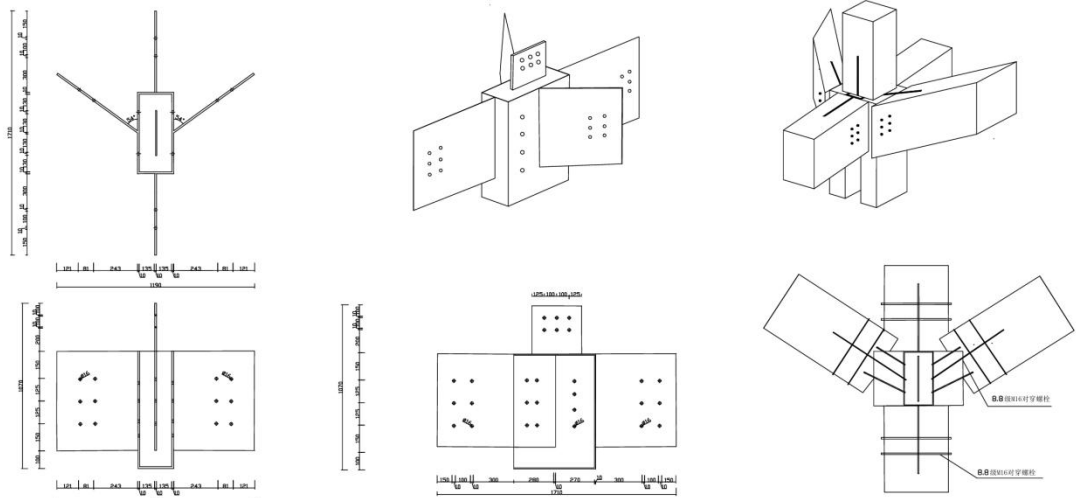


图 6.3III号节点设计图

6.3.4 IV号节点螺栓设计

(1) 恒载:

屋面自重： $7 \times 0.175 \times 5 \times 2 = 12.25 \text{ kN}$

梁自重： $7 \text{ kN/m}^3 \times 5 \times 0.45 \times 0.6 \times 3 = 18.9 \text{ kN}$

荷载组合： $1.3 \text{ 恒载} + 1.5 \text{ 活载} = 18.61 \text{ kN}$

IV号节点设计图如下。

节点详图IV

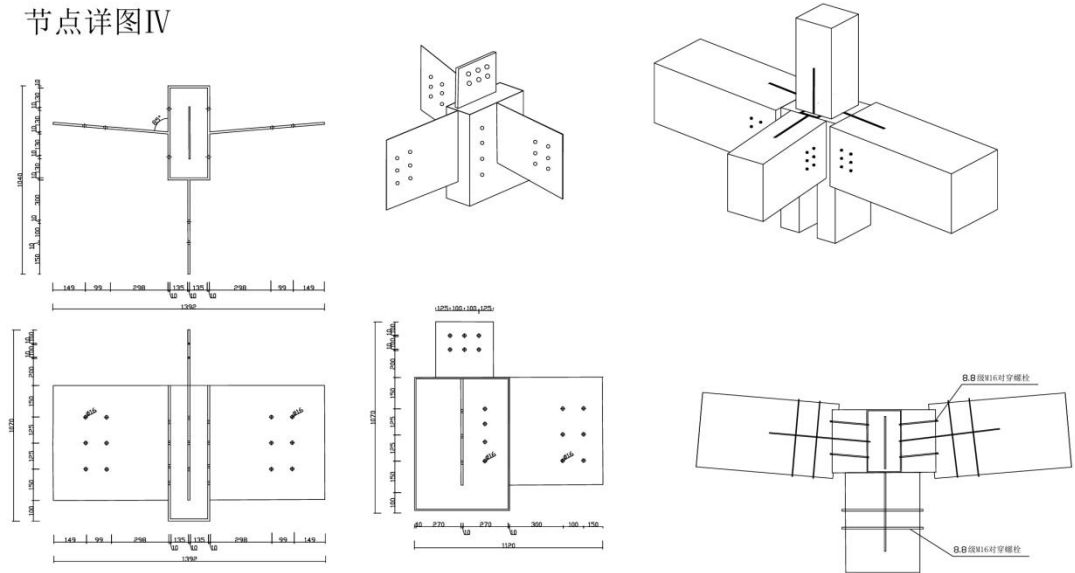


图 6.4IV号节点设计图

6.3.5 V号节点螺栓设计

(1) 恒载:

屋面自重： $7 \times 0.175 \times 5 \times 2 = 12.25 \text{ kN}$

梁自重： $7 \text{ kN/m}^3 \times 5 \times 0.45 \times 0.6 \times 3 = 18.9 \text{ kN}$

荷载组合：1.3恒载+1.5活载=19.34 kN

V号节点设计图如下。

节点详图V

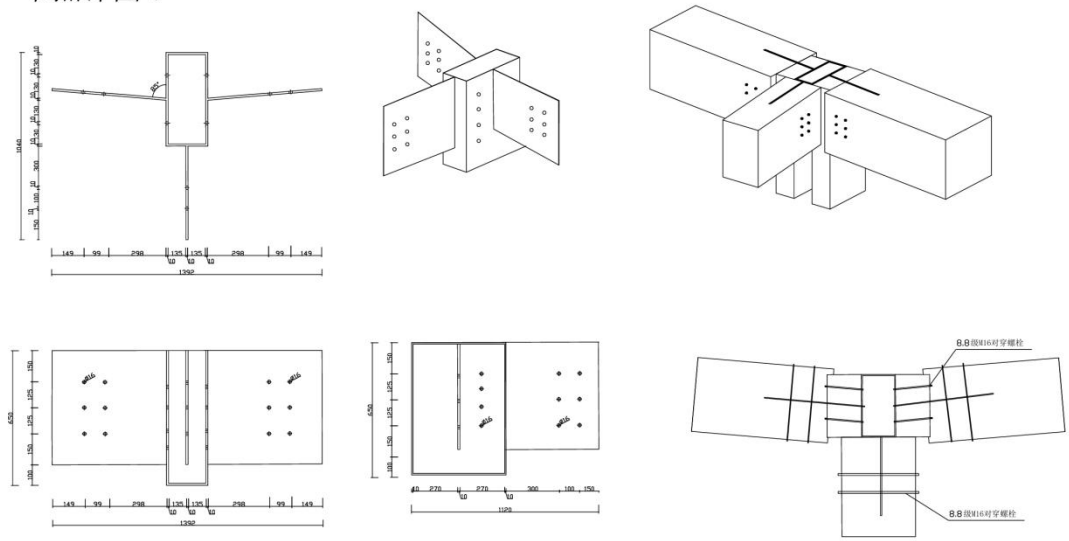


图 6.5 V 号节点设计图